

1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16

The legacy of C₄ evolution in the hydraulics of C₃ and C₄ grasses

Haoran Zhou^{1,2,3}, Erol Akçay¹, Erika Edwards², Brent Helliker¹

¹Department of Biology, University of Pennsylvania, Philadelphia, PA 19104, USA

²Department of Ecology and Evolutionary Biology, Yale University, New Haven, CT 06511, USA

³University Corporation for Atmospheric Research, Boulder, CO 80301, USA

Correspondence: Haoran Zhou

Phone: 1-215-808-7042

Email: haoran.zhou@yale.edu

Erol Akçay: *eakcay@sas.upenn.edu*

Erika Edwards: *erika.edwards@yale.edu*

Brent R. Helliker: *helliker@sas.upenn.edu*

17 **Abstract**

18 The anatomical reorganization required for optimal C₄ photosynthesis should also impact plant
19 hydraulics. Most C₄ plants possess large bundle-sheath cells and high vein density, which should
20 also lead to higher leaf hydraulic conductance (K_{leaf}) and capacitance. Paradoxically, the C₄
21 pathway reduces water demand and increases water-use-efficiency, creating a potential mis-
22 match between supply capacity and demand in C₄ plant water relations. We use phylogenetic
23 analyses, physiological measurements, and models to examine the reorganization of hydraulics
24 in closely-related C₄ and C₃ grasses. Evolutionarily young C₄ lineages have higher K_{leaf} ,
25 capacitance, turgor-loss-point, and lower stomatal conductance than their C₃ relatives. In
26 contrast, species from older C₄ lineages show decreased K_{leaf} and capacitance, indicating that
27 over time, C₄ plants have evolved to optimize hydraulic investments while maintaining C₄
28 anatomical requirements. The initial “over-plumbing” of C₄ plants disrupts the positive
29 correlation between maximal assimilation rate and K_{leaf} , decoupling a key relationship between
30 hydraulics and photosynthesis generally observed in vascular plants.

31

32 **Introduction**

33 The evolution of C₄ photosynthesis in the grasses— and the attendant fine-tuning of both
34 anatomical and biochemical components across changing selection landscapes^[1,2,3]— likely
35 impacted leaf hydraulics and hydraulics-photosynthesis relationships, both within the grass
36 lineages in which C₄ evolved independently > 20 times^[4], and as compared to closely-related
37 C₃^[5,6]. C₄ plants typically exhibit lower stomatal conductance (g_s) and consequently greater
38 water-use efficiency than C₃, because the concentration of CO₂ inside bundle sheath cells permits
39 reduced intercellular CO₂ concentrations and conservative stomatal behavior^[7,8,9]. At the same
40 time, C₄ plants require high bundle sheath to mesophyll ratios (BS:M), which are accomplished
41 with increased vein density and bundle sheath size as compared to C₃ plants. In C₃ species, leaf
42 hydraulic conductance (K_{leaf}) has a positive relationship with vein density^[10,11,12,13]. The
43 decreased inter-veinal distance and consequently higher vein density in C₄ species has been
44 predicted to lead to a higher K_{leaf} than closely-related C₃ species^[14,15]. Further, increased bundle
45 sheath size was proposed to lead to a higher leaf capacitance in C₄ species^[15,16]. This would lead
46 to a potential physiological “mis-match”, where the evolution of the C₄ pathway simultaneously
47 increases a plant’s hydraulic capacity while reducing its transpirational demand.

48

49 The significance of such a potential physiological mismatch depends on the potential costs and
50 tradeoffs associated with the building of an ‘over-plumbed’ leaf. If the costs are high^[12,17], then
51 one would expect to see a reduction of K_{leaf} over evolutionary time, as continued selection works
52 to optimize the C_4 metabolism^[5,18]. Alternatively, a maintenance of high K_{leaf} over time could
53 result from either a lack of strong selection to reduce K_{leaf} , or a strong evolutionary constraint
54 imposed by the anatomical requirements of C_4 photosynthesis. In other words, the high BS:M
55 ratio required for an efficient C_4 system may directly limit the ability of C_4 plants to optimize
56 their hydraulic architecture.

57

58 The evolution of a new photosynthetic pathway that results in multiple potential changes to the
59 plant hydraulic system represents the ideal platform to expand our understanding of the
60 relationship between photosynthesis and water transport. It is generally thought that maximum
61 photosynthetic rate (A_{max}) and hydraulic capacity (K_{leaf}) are tightly linked, because the ability to
62 transport water through leaves to the sites of evaporation at a high rate allows for the
63 maximization of carbon gain. Studies have documented a positive correlation between A_{max} and
64 K_{leaf} across many scales, from a broad phylogenetic spectrum of species spanning vascular
65 plants^[11], to smaller clades of closely related species^[13]. Grasses are largely absent from previous
66 efforts to examine this relationship, which is unfortunate because of the parallel venation found
67 in grasses and other monocots. With over 20 origins of C_4 photosynthesis with ages that span ~
68 30 million years, grasses also present a unique opportunity to examine the influence of C_4
69 evolution on A_{max} - K_{leaf} relationships. Using a broad sampling of grasses (Fig. 1), we determined
70 whether anatomical differences associated with C_4 evolution result in greater K_{leaf} and leaf
71 capacitance compared to their C_3 relatives. We then compared these properties between closely
72 related C_3 and C_4 clades to determine how C_4 evolution alters the predicted A_{max} - K_{leaf}
73 relationships. Finally, we then quantified evolutionary trends in K_{leaf} , capacitance and turgor loss
74 point after the evolution of C_4 within a lineage by asking whether more recent origins of C_4 are
75 represented by higher K_{leaf} and a greater K_{leaf} - A_{max} mismatch.

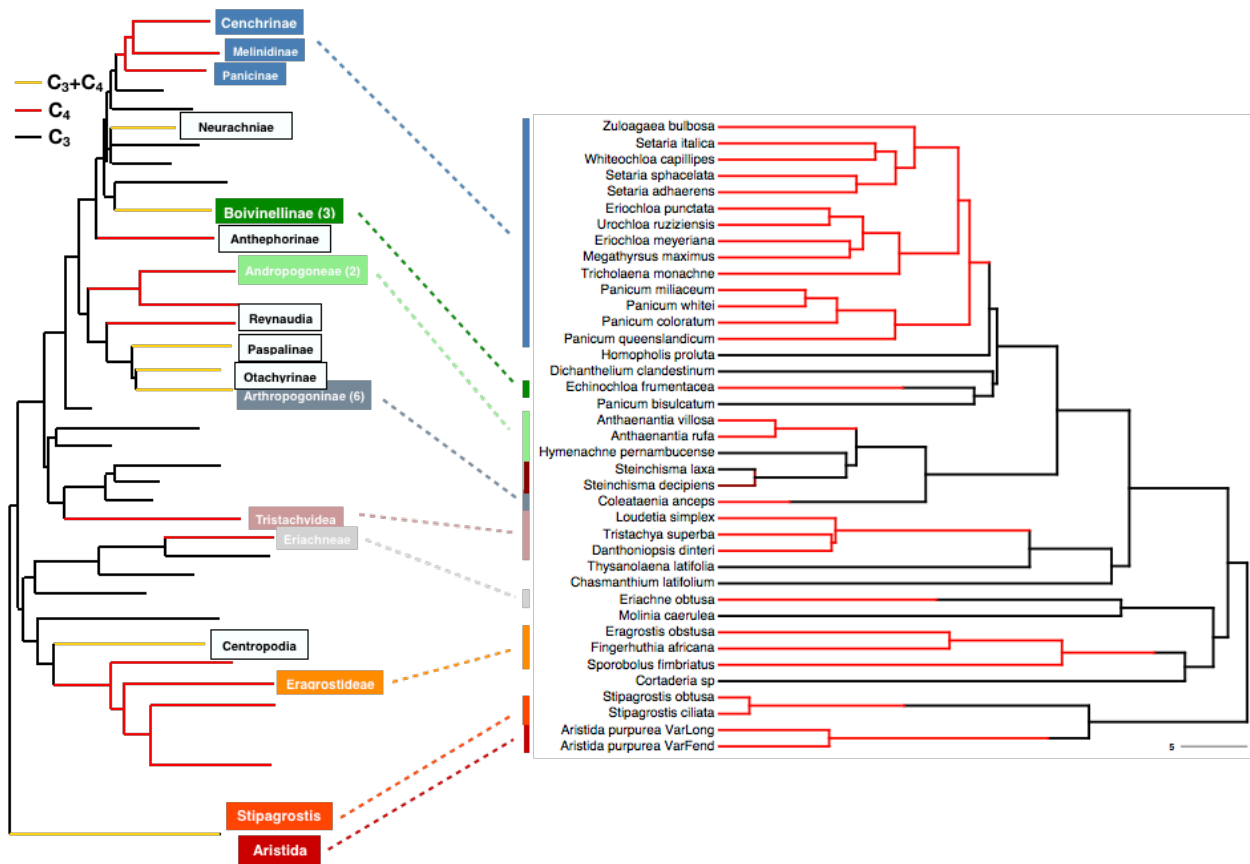
76

77 **Results**

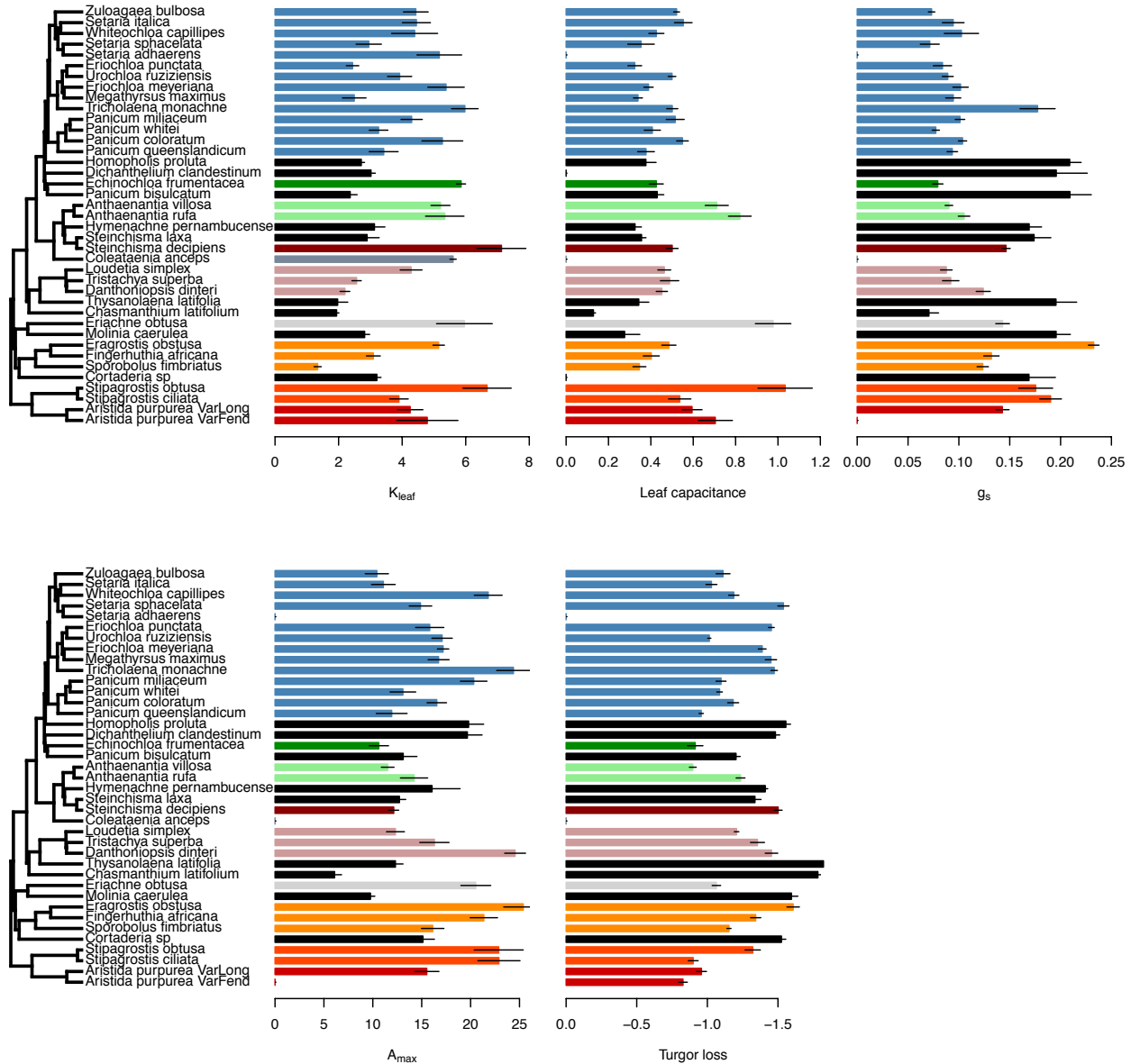
78 Within each phylogenetic cluster, there were no clear patterns between C₃ and C₄ hydraulic traits
79 by conducting ANOVA tests only. C₄ grasses had higher or equivalent K_{leaf}, leaf capacitance
80 leaf turgor loss point, A_{max} and lower or equivalent g_s than their closest C₃ relatives (Fig. 2). The
81 one C₃-C₄ intermediate species, *Steinchisma decipiens*, in our analysis had K_{leaf} similar or
82 equivalent to C₄, but leaf capacitance, leaf turgor loss point, g_s and A_{max} equivalent to C₃ (Fig. 2).
83 By analyzing our data in the context of the evolutionary models (Supplementary Table S1),
84 however, we found clear C₃-C₄ differences in most measured traits. We first fitted evolutionary
85 models of Brownian motion and Ornstein-Uhlenbeck processes to the hydraulic traits based on a
86 reliable dated phylogenetic tree^[19]. The best fitting evolutionary model to the data for K_{leaf}, leaf
87 turgor loss point, A_{max} and g_s was Ornstein-Uhlenbeck model, while the Brownian model is the
88 best-fitting model for leaf capacitance, as determined by the AICc and Akaike weights and LRT
89 test (Table 1, Supplementary Tables S2-S6). Higher K_{leaf}, higher A_{max}, lower leaf turgor loss
90 point, and lower g_s are detected C₄ species compared to C₃ (LRT test, all $p < 0.01$; all $\Delta AICc < -3$).
91 For leaf capacitance, there is no significant difference for C₃ and C₄ species.

92
93 We also looked for evolutionary trends in hydraulic traits after the evolution of a C₄ system to
94 probe for an extended ‘optimization’ phase of C₄ evolution^[3, 20]. Identifying directional trends in
95 continuous character evolution is difficult without fossil taxa, and it is impossible to directly
96 measure hydraulic traits for fossils; however, we can test for trends indirectly using extant
97 species. For example, if reduction in K_{leaf} is selected for subsequent to C₄ evolution we expect
98 older C₄ lineages to have lower K_{leaf} values than younger C₄ lineages. We extracted the
99 evolutionary age of C₄ origin for each of our lineages from the dated phylogeny^[19]. Regressions
100 of evolutionary age versus hydraulic traits provide strong evidence for a long-term directional
101 trend in hydraulic evolution following the origin of C₄ photosynthesis (Fig. 3). K_{leaf}, leaf turgor
102 loss point and capacitance showed significant negative correlations with evolutionary age, while
103 A_{max} had a significant positive correlation. In contrast, there was no significant relationship
104 between g_s and evolutionary age. No evolutionary relationships were detected in C₃ species,
105 which indicated the correlations between evolutionary age and hydraulic traits were unique to C₄
106 species. We also tested for an evolutionary trend by modelling hydraulic trait evolution using a
107 phylogeny with branch lengths scaled to molecular substitutions/site, which provides an estimate
108 of differences in evolutionary rates between lineages^[4]. While the second approach requires

109 many assumptions that are likely violated, the results also provide additional support to a
 110 directional trend in K_{leaf} and capacitance in C_4 lineages: comparing 12 different types of models
 111 with or without evolutionary trends (supplementary Table S7), we found K_{leaf} and leaf
 112 capacitance were best fitted by the Brownian motion model with a significant negative trend for
 113 C_4 (Supplementary Table S8, Table S9-13).
 114
 115



116
 117 Fig. 1 Phylogenetic sampling of the species for measuring physiological traits and the
 118 independent evolutionary lineages corresponding to grass lineages. The figure on the left was a
 119 grass phylogeny adapted from GPWGII (2012), on which the tags represent the recommended
 120 independent evolution of C_4 for comparative studies in grasses (numbers represent there are
 121 multiple origins within a lineage). The figure on the right is the phylogeny for our species,
 122 extracted from a dated phylogeny ^[19] for species sampled in our experiments. We sampled nine
 123 independent evolution of C_4 in total.
 124



125

126

127 Fig. 2 Hydraulic conductance (K_{leaf} , mmol m⁻² s⁻¹ MPa⁻¹), leaf capacitance (mmol m⁻² MPa⁻¹),
 128 maximal stomatal conductance (g_s , mmol m⁻² s⁻¹), maximal assimilation rate (A_{max} , μmol m⁻² s⁻¹),
 129 and leaf turgor loss points (Turgor loss, -MPa) of closely related C₃ and C₄ species. Different
 130 colored clusters of bars show nine different origins of closely-related C₃ and C₄ species. C₃
 131 species are colored black. Error bars indicated standard errors.

132

133 Table 1 Phylogenetic results of the best-fitted models and their parameters for hydraulic
134 conductance (K_{leaf}), leaf capacitance (Capacitance), stomatal conductance (g_s), and leaf turgor
135 loss point (Turgor loss) (summarizing Table S2-S6; model description: Table S1).

136

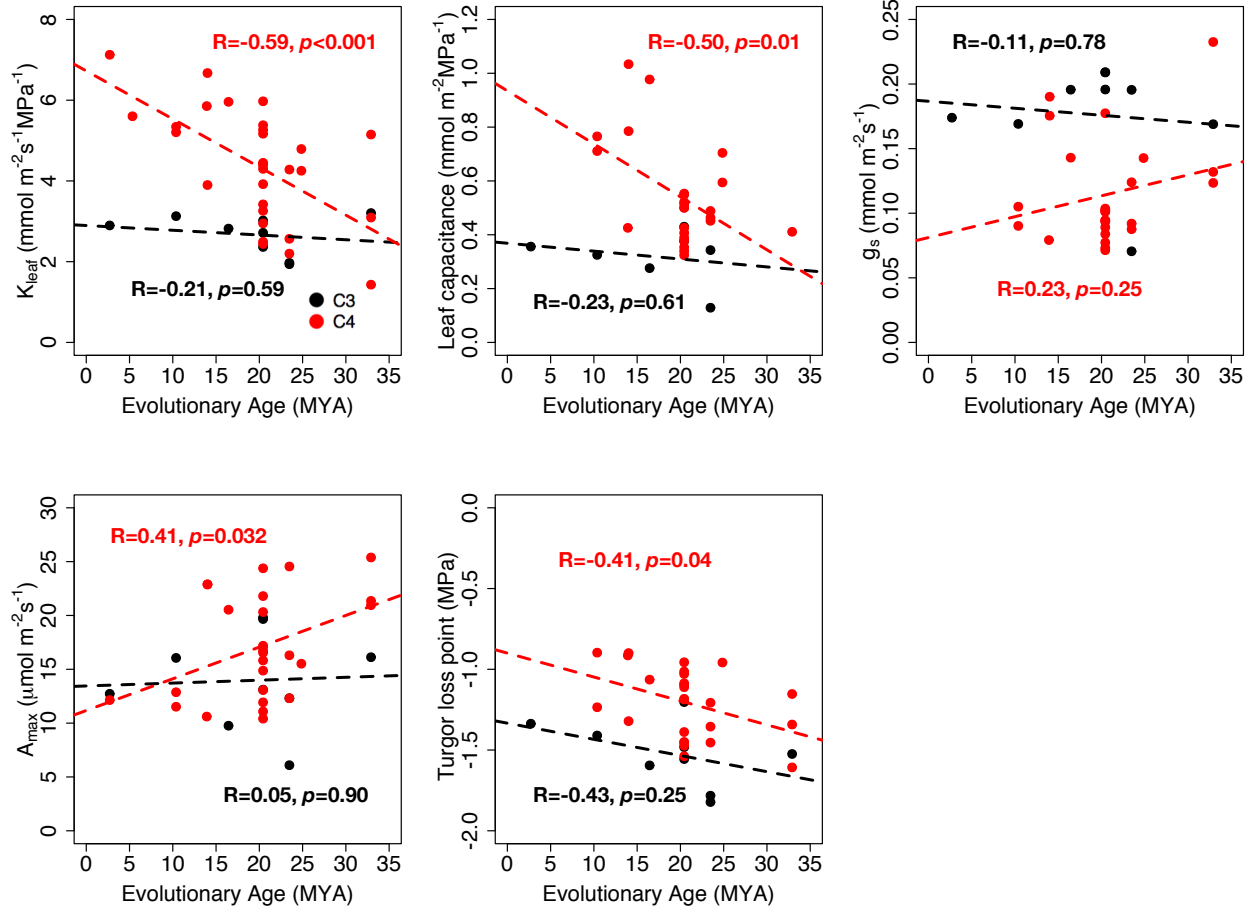
Property	Model	Model type	AICw	Root/Theta	
				C ₃	C ₄
K_{leaf}	Model 6*	OU2	0.984	2.682	4.295
Capacitance	Model 2	BM1	0.323	0.523	
g_s	Model 6*	OU2	0.980	0.183	0.102
Turgor loss	Model 6*	OU2	0.996	-1.522	-1.192
A_{max}	Model 6*	OU2	0.5292	13.66	17.34

137 * indicates the model fit significantly better than all the other models. Different root or theta values for C₃
138 and C₄ indicates that the evolutionary model with two different values of the root or theta for C₃ and C₄
139 species is a significantly better fit than the evolutionary model with the same root or theta.

140

141 We next explored how A_{max} and hydraulic traits are correlated across the phylogeny, and whether
142 this relationship is different for C₃ and C₄ lineages. The correlations between A_{max} and K_{leaf} were
143 different between C₃ and C₄ (Fig. 4, Table 2, Table S13). A_{max} was significantly positively
144 correlated with K_{leaf} for C₃, but not for C₄ (Fig. 4, Table 2, Table S13). A_{max} was weakly
145 positively correlated with leaf capacitance and g_s and the correlations were not significantly
146 different for C₃ and C₄ (Fig. 4, Table 2, Supplementary Table S21, S22). A_{max} was negatively,
147 but not significantly related with leaf turgor loss point in C₃ and C₄ species (Supplementary
148 Table S23).

149



150

151

152 Fig. 3 The regression for hydraulic conductance (K_{leaf}), leaf capacitance, leaf turgor loss point,
 153 stomatal conductance (g_s) and maximal assimilation rate (A_{max}) vs. the evolutionary age for the
 154 nine origins of C₄ to show the evolutionary trend within C₄ and within their closely-related C₃
 155 species. The evolutionary age for each sampled origin is derived from the dated phylogeny^[19].

156

157

158 Table 2 Phylogenetic Correlations between maximal assimilation rates (A_{max}) and hydraulic traits
 159 for C₃ and C₄ species (summarizing Table S20-S23; model description: Table S19).

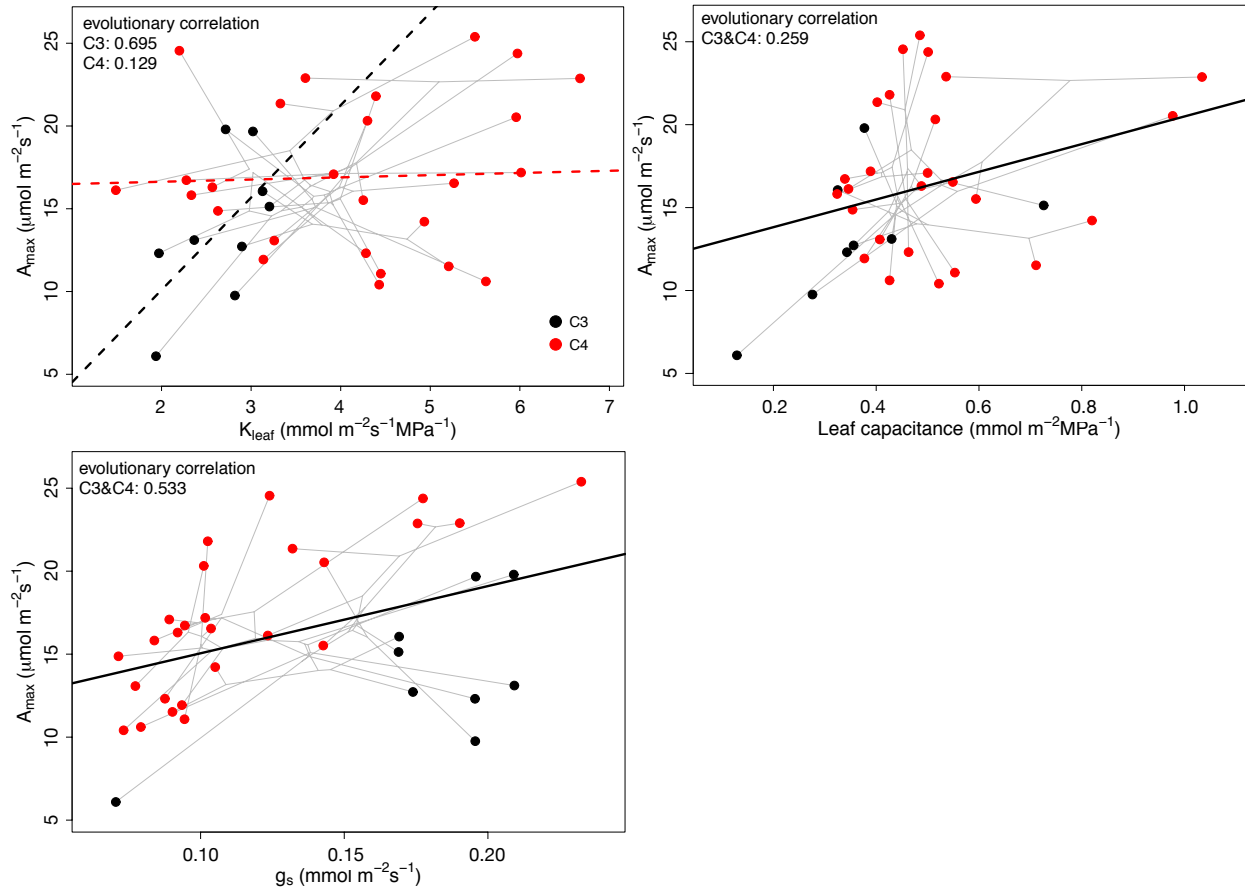
Parameter 1	Parameter 2	Best Model	r for C ₃	r for C ₄	p value
A_{max}	K_{leaf}	CorModel 3	0.695	0.129	0.012/0.51
A_{max}	Capacitance	CorModel 2	0.259		0.027
A_{max}	g_s	CorModel 1	0.533		0.003

A_{\max}	leaf turgor loss	CorModel 1	-0.223	0.256
------------	------------------	------------	--------	-------

160 Different r means the best fitted model assuming different correlations for C_3 and C_4 . One r means the
161 best fitted model assuming similar correlations for C_3 and C_4 . p values indicated whether the correlation
162 coefficients are significant.

163
164 We used our mechanism-based physiological model^[32] to consider how the evolution of higher
165 K_{leaf} would affect the optimal g_s and photosynthesis in C_3 and C_4 plants. An increase in K_{leaf} in
166 the C_3 ancestor selects for higher g_s and increases the steady-state leaf water potential to a
167 limited extent (Fig. 5, S1). Changing K_{leaf} has a smaller effect on the photosynthesis rate of C_4
168 than that of C_3 (Fig. 6, Table S25). Decreasing K_{leaf} by half or doubling it changes the
169 photosynthesis rate of a C_4 plant by an average of -4.27% and 3.48%, respectively. In contrast,
170 the same shifts in K_{leaf} has average effects of -10.07% and 9.14% on the assimilation rate of a C_3
171 plant. The sensitivity of the assimilation rate to changes in K_{leaf} decreases with increasing CO_2
172 concentration and increasing water-limitation for both C_3 and C_4 plants (Table S25). These
173 differences in sensitivity to K_{leaf} were robust to differences in physiological properties between
174 C_3 and C_4 (specifically, the temperature response properties and J_{\max}/V_{cmax} ratio; Table S25). The
175 assimilation rate of C_4 plants was still less sensitive to K_{leaf} than that of C_3 species under
176 different CO_2 concentration and water-limited conditions (Table S25). The physiological
177 modeling results indicates that C_4 species maintain lower g_s and higher leaf water potential
178 compared to closely related C_3 species because the CCM reduces transpirational demand. The
179 modeling effects of varying K_{leaf} on photosynthesis confirmed the diminished returns for high-
180 efficiency water transport in C_4 species mentioned above.

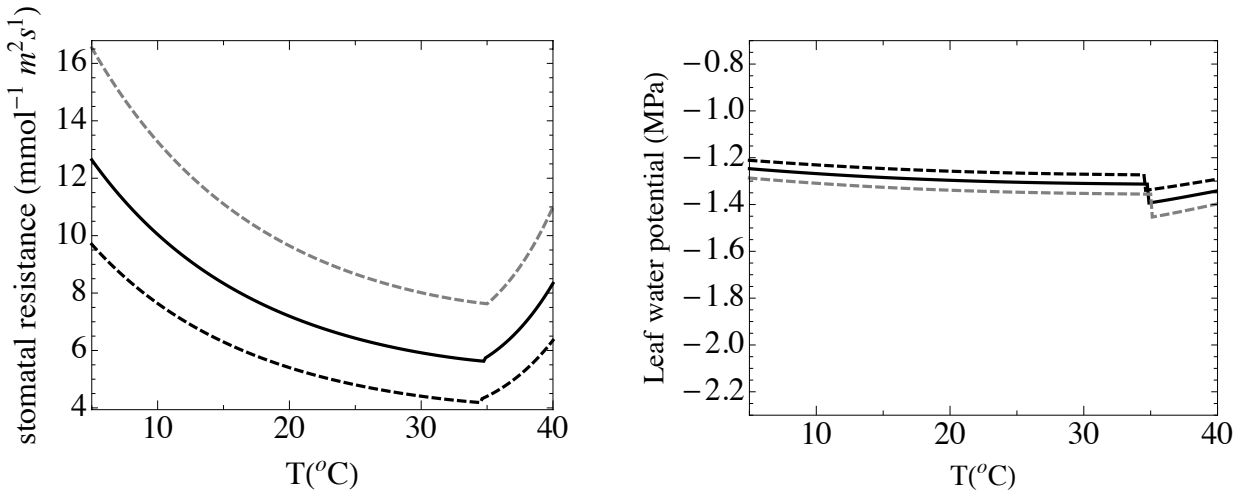
181



182

183 Fig. 4 Phylogenetic correlation for C₃ and C₄ between A_{max} and other hydraulic traits (K_{leaf} , leaf
184 capacitance and g_s). Different/same correlation values on the figure mean C₃ and C₄ have
185 significantly different/same correlations. Detailed phylogenetic correlation models and analysis
186 results are shown in Table 2. Dashed black line: C₃; dashed red line: C₄; solid black line: C₃ and
187 C₄ have the same correlation; grey lines indicate the phylogeny.

188



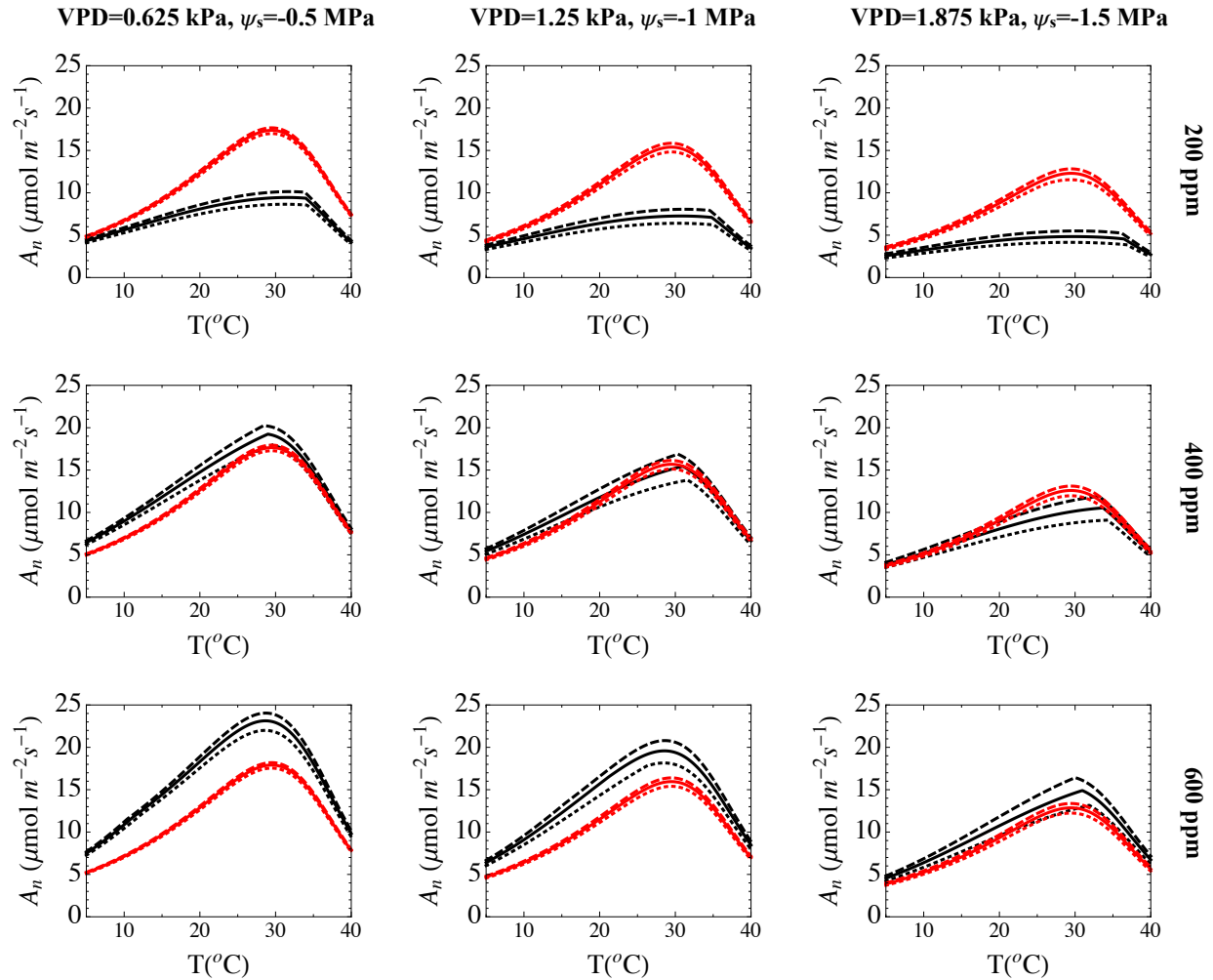
189

190 Fig. 5 The effect of changing K_{leaf} on stomatal resistance (the inverse of g_s) and leaf water
191 potential under $\text{VPD}=1.25$ kPa, $\psi_s = -1$ MPa and CO_2 concentration of 200 ppm for the C_3 model.
192 Solid black line: measured K_{leaf} , dashed black line: K_{leaf} doubled; dashed grey line: K_{leaf} reduced
193 by 50%.

194

195 To see if C_4 subtypes varied in hydraulic traits and their evolutionary rates or variance, we also
196 considered evolutionary models where we allowed each variable to have a subtype-specific value
197 (Supplementary Table S1). We found no significant differences in K_{leaf} , leaf capacitance, g_s ,
198 leaf turgor loss point and A_{max} among C_4 subtypes (all $\Delta\text{AICc} > 0$, ΔAICc obtained by AICc of
199 subtype models minus AICc model not considering subtypes; Supplementary Tables S14-18).
200 Although different decarboxylation enzymes are utilized by the three major subtypes (NADP-
201 ME, NAD-ME and PCK), there does not seem to be an evolutionary effect on hydraulic traits.
202 However, a previous study documenting PCK species from the Chloridoideae and Panicoideae
203 lineages with lower leaf turgor loss point^[23]. Such differences were not apparent when we
204 compared C_4 subtypes with multiple lineages. Our current representation of different subtypes is,
205 however, somewhat limited. It would be advantageous to increase both lineage and species
206 diversity and to balance subtypes within lineages to more deeply examine C_4 subtypes.

207



208

209 Fig. 6 Modeling results of photosynthesis rates along with different CO₂ concentration, different
 210 temperatures and different water limited conditions for C₃ (black lines) and for C₄ (red lines).

211 Solid lines: modeling results for C₃ and C₄ with measured leaf hydraulic conductance; dashed
 212 lines: modeling results for C₃ and C₄ with twice of the regular leaf hydraulic conductance; dotted
 213 lines: modeling results for C₃ and C₄ with half of the regular leaf hydraulic conductance. C₃ and
 214 C₄ parameters are kept the same except for C₄ has the carbon concentration mechanism.

215

216

217 Discussion

218 The evolution of the C₄ pathway in the grasses caused a series of shifts in hydraulic properties as
 219 compared to closely-related C₃ grasses. The anatomical requirements of C₄ initially increased
 220 K_{leaf} and leaf capacitance, as predicted by previous studies^[14,15,16]; however, K_{leaf} and leaf

221 capacitance appear to decline over evolutionary time, suggesting a long period of physiological
222 optimization after the initial assembly of a new photosynthetic system. Previous examination of
223 leaf hydraulic traits in grasses focused on investigating single species or were not developed
224 within a phylogenetic framework when comparing multiple species^[21,22], and phylogenetic
225 studies have assumed trait evolution as simple Brownian motion^[23,24]. Hydraulic traits, however,
226 may have evolved along different trajectories before and after the evolution of the C₄ pathway
227 and associated anatomical reorganization, resulting in more complicated evolutionary dynamics.
228 Our evolutionary models indicated C₄ grasses initially had higher K_{leaf}, leaf capacitance, turgor
229 loss point than corresponding C₃, and a lower stomatal conductance (g_s) than grasses consistent
230 with previous studies^[25,26]. Decreased vein distance and increased bundle sheath size are thought
231 to be anatomical precursors to the evolution of C₄^[27,28], and both are thought to increase K_{leaf}
232 and/or leaf capacitance^[14,15]. Therefore, the shifts of K_{leaf} and leaf capacitance likely occurred
233 before, or at the initial formation of, the C₄ CCM. After the full formation of C₄, K_{leaf} and/or leaf
234 capacitance started to decrease, which led to higher or equivalent K_{leaf} and leaf capacitance in the
235 current C₃ and C₄ species (Fig. 2). Liu et al. (2019) found that K_{leaf} in C₄ grasses overlapped with
236 C₃ values^[24]. The positive correlation between A_{max} and the evolutionary age also supports an
237 extended optimization phase for C₄. Previous studies have indicated that species from the oldest
238 C₄ lineages (*Chloridoideae* and *Andropogoneae* for example) contain the most productive crops
239 (Sage, 2016), while some recent C₄ lineages are not more productive than C₃ (Ripley et al., 2008;
240 Lundgren et al., 2016). In contrast, the significant decrease of g_s and the increase of leaf turgor
241 loss point occurred with the evolution of a fully operational C₄ CCM, as suggested by our
242 physiological models discussed below. Consistent with this prediction, in clades that possess a
243 range of C₃, C₃-C₄ intermediate and C₄ physiologies, the increased water use efficiency,
244 decreased g_s, and a broadened ecological niche are observed only in plants with a full C₄
245 CCM^[29,30].

246
247 The evolution of C₄ significantly alters the widely-accepted A_{max}-K_{leaf} relationships existing in
248 vascular plants. A_{max} is limited by the efficient transport of water through leaves to replace water
249 loss through open stomata, which is the likely cause of a positive correlation between K_{leaf} and
250 A_{max} across and within plant taxa^[11,13,31]. We found that A_{max} and K_{leaf} are positively correlated
251 in our C₃ species but not in C₄ (Fig 4). Ocheltree et al. (2016)^[22] similarly found no relationship

252 between K_{leaf} and A_{max} in a set of nine C_4 species. We see possible explanations that are not
253 necessarily mutually exclusive. First, the positive relationship of A_{max} and K_{leaf} is weakened
254 under high K_{leaf} , possibly due to diminished returns of further increasing the efficiency of water
255 transport^[11,31], a conclusion supported by our physiological modeling results below. As K_{leaf}
256 tends to be lower in grasses than in other species, it is possible that the diminishing returns from
257 increasing K_{leaf} manifest at lower values in grasses, and the initial high K_{leaf} resulting from C_4
258 anatomy could be in the A_{max} “saturation” zone. Lastly, we see evidence here that the time-since-
259 C_4 -evolution affects several hydraulic traits across and within lineages, and it could be that a
260 walk towards $A_{\text{max}}-K_{\text{leaf}}$ optimality is slowly occurring within C_4 grass lineages in relatively
261 newfound ecological niches. However, the similar correlations of g_s vs. A_{max} in C_3 and C_4 and
262 lack of evolutionary trend in g_s indicated the evolutionary processes of g_s might be already near
263 the optimal condition or stabilized quickly. Other hydraulic traits of leaf capacitance and leaf
264 turgor loss point do not seem to contribute to the A_{max} directly because of weak correlations.

265
266 We identified the mode and direction of evolution for hydraulic traits in C_3 and C_4 lineages and
267 found evidence that different traits followed different evolutionary processes. Hydraulic
268 conductance and leaf capacitance could therefore evolve with directions in a step-wise fashion
269 due to anatomical constraints, but g_s and leaf turgor loss point might have a more quick process
270 of readjustments, which allows them to stabilize soon. This suggests that there could be greater
271 diversification of K_{leaf} and leaf capacitance in the existing C_4 species and maybe in the future.
272 Also, these rearrangements of hydraulic properties interacted with each other throughout the
273 evolutionary trajectory. For example, increased K_{leaf} and leaf capacitance would lead to an
274 increased water transport efficiency, which enabled greater g_s of the C_4 ancestor (either a C_3
275 grass or a C_3 - C_4 intermediate), but the formation of the full C_4 CCM enables a decrease of g_s .
276 Therefore, observed g_s in C_4 grasses reflects a balance of these two contrasting physiologies
277 playing out in a given ecological and phenological background, which may explain why although
278 C_4 g_s was lower than the C_3 , the difference was not large. This line of reasoning might also
279 explain the inconsistent observations of g_s comparisons between C_3 and C_4 . Most previous
280 studies found that C_4 grasses had lower g_s than C_3 grasses in both closely related and unrelated
281 species^[25,33], yet Taylor et al. (2014) found that C_4 grasses maintained a higher or equivalent g_s
282 to closely-related C_3 grasses^[34]. Likewise, artificial selection or genetic engineering might have

283 more success in adjusting these hydraulic traits in advance. Consciously selecting or
284 manipulating narrower xylem, decreasing the expression of aquaporins, or other mechanisms of
285 decreasing leaf conductance while maintain high bundle sheath to mesophyll ratio, together with
286 CCM may increase the water use efficiency of C₄ species further. Our phylogenetic analyses can
287 thus inform both the evolutionary history of C₄ plants and future efforts to modify C₄ crops.

288

289 By capitalizing on the multiple origins of C₄ photosynthesis in grasses, we have shown that the
290 vascular organization that is a hallmark of C₄ plants also impacts leaf hydraulics, and disrupts the
291 established link between hydraulic and photosynthetic capacity demonstrated in C₃ plants. C₄
292 grasses are “overplumbed” relative to their C₃ counterparts, suggesting that the costs associated
293 with the production of an extensive leaf vasculature require re-evaluation in plants with C₄
294 photosynthetic systems. The gradual decline in K_{leaf} in C₄ lineages over millions of years also
295 requires an explanation. The C₄-K_{leaf} conundrum provides an opportunity to examine what we
296 mean by “evolutionary constraint” and highlights the very dynamic nature of evolutionary trade-
297 offs and functional optimization. First, we assume that the costs of building and maintaining a
298 high K_{leaf} are still significant in C₄ plants^[12,35,36,37,38]. The most efficient way to reduce K_{leaf} costs
299 would be to reduce venation density, as veins come with high construction costs^[12,17], and also
300 reduce the leaf area that is available for carbon fixation. Yet the anatomical requirements of the
301 C₄ system preclude this option: reducing vein density would result in a highly inefficient C₄
302 system^[15], which would negatively impact the plant’s carbon budget, presumably to a much
303 greater extent than the cost of an overbuilt venation system. As vein construction is a primary
304 contribution to the cost of a high K_{leaf}, and high vein densities are now linked to a new function
305 (C₄ carbon fixation), the cost-benefit calculations in optimizing K_{leaf} have shifted, and the
306 tradeoff is in favor of overplumbing in order to maintain a highly efficient new carbon fixation
307 system. In evolutionary vocabulary, what emerges is a new constraint – and in this example, it is
308 clear that the emergence of a new constraint to organismal evolution is simply due to a shift in
309 the tradeoffs associated with characters that influence multiple aspects of organismal function. In
310 other words, we assume a low vein density is a phenotype that is still developmentally
311 achievable for C₄ grasses; what has prevented its emergence is the shift in functional costs
312 associated with reduced vein densities.

313

314 And yet, we documented a gradual reduction in K_{leaf} over time, which we presume was
315 accomplished via changes in other factors that influence leaf hydraulic capacity— perhaps by
316 changing xylem conduit diameters, shifts in extra-xylary mesophyll conductance, decreased
317 expression of aquaporins, and reorganization of internal air spaces^[6,12,37,39,40]. It is possible that
318 these changes resulted from a continued and direct selection pressure to reduce investment in an
319 underutilized hydraulic system. An alternative explanation is that all of the traits that influence
320 K_{leaf} also play important roles in other aspects of leaf function – and the emergent of a new
321 constraint (a high vein density to maintain C_4 function) has *released* still other constraints on
322 other traits so that they may be optimized for their other functions. A striking pattern in our data
323 is that older C_4 lineages have achieved both lower K_{leaf} and higher A_{max} – suggesting that they
324 are continuing to optimize their photosynthetic capacity, long after the initial origin of C_4 . We
325 suspect that the slow evolutionary decline in K_{leaf} is due in large part to the optimization of traits
326 to increase A_{max} at the expense of K_{leaf} , which is possible only because hydraulic capacity was
327 already “buffered” by the vein density requirements of C_4 – allowing for continued reductions of
328 K_{leaf} at no functional cost. Increased suberization of bundle sheath cells is one example of a
329 potential release of constraint^[22]: it allows C_4 plants to gain higher A_{max} through reducing bundle
330 sheath leakiness, but it likely simultaneously reduces water flow from veins out into the
331 mesophyll. Since C_4 plants are already operating in hydraulic excess, bundle sheath suberization
332 may be optimized for C_4 function without any negative repercussions for plant water relations.
333 This hypothesis could also explain the opposing trends in A_{max} and K_{leaf} when viewed as a
334 function of evolutionary age. The examination of C_4 evolution in grasses provides an exciting
335 system to study the evolutionary dynamics of constraints highlighted by the interplay between
336 photosynthesis and plant hydraulics.

337

338 **Methods**

339 ***Plant material***

340 We collected seeds of 39 closely related C_3 (9 species), C_4 species (29 species), representing
341 three C_4 subtypes, nine C_4 origins, and one C_3 - C_4 intermediate species. The selected C_3 and C_4
342 species fall into nine identified C_4 lineages belong to the 11 recommended grass lineages for C_3
343 and C_4 study (11 out of the total 24 grass lineages have clear C_3 sister species and are
344 recommended for comparative studies in GPWGII, 2012^[4]): *Aristida*, *Stipagrostis*,

345 *Chloridoideae* (*Eragrostideae*), *Eriachne*, *Tristachyideae*, *Arthropogoninae*, *Otachyrinae*
346 (*Anthaenantia*), *Panicinae*, *Melinidinae*, and *Cenchrinae* (Fig. 1). In 2015, seeds were surface
347 sterilized before germination and the seedlings were transferred to 6 inch pots with the soil of
348 Fafard #52 (Sungro, Ajawam, MA). Six replicates of each species were randomized in the
349 greenhouse of the University of Pennsylvania supplemented with artificial lighting. The plants
350 were watered twice daily. Daytime/night temperature was controlled at 23.9-29.4/18.3-23.8 °C;
351 relative humidity was around 50-70%. Plants were fertilized once per week with 300 ppm
352 Nitrogen solution (Jacks Fertilizer; JR Peters, Allentown, PA) and 0.5 tsp of 18-6-8 slow release
353 Nutricote Total (Arysta LifeScience America Inc, NY) per pot was applied when plants were
354 potted into 6 inch pots. To maintain optimal plant growth a 15-5-15 cal-mg fertilizer was used
355 every third week. All measurements were performed on the most-recent fully expanded leaves.
356

357 ***Hydraulic traits***

358 Leaf hydraulic conductance (K_{leaf}) was measured using the evaporative flux method^[41], with
359 some adjustments to maintain stability of the evaporative environment to which the leaf was
360 exposed (Supplementary Methods). The evening before measurements, potted plants were
361 brought to the laboratory, watered, and then covered by black plastic bags filled with wet paper
362 towels to rehydrate overnight. For the leaf gasket, a 1 cm diameter, ~ 1 cm long solid silicone
363 rubber cylinder was cut nearly in two, leaving a hinge on one end. The cylinder was placed
364 around the leaf blade near the ligule and glued shut with superglue^[42]. The leaf was cut from the
365 plant with a razor blade while submerged in a 15 mmol L⁻¹ KCl solution; the rubber gasket was
366 then attached to tubing filled with the same KCl solution. The other end of the tubing was inside
367 a graduated cylinder that sat on a digital balance (Mettler-Toledo). The leaf was then placed
368 inside a custom, environmentally controlled cuvette that allowed for the measurement of entire
369 grass blades. Throughout measurements, cuvette temperature was controlled at 25 °C and the
370 humidity was 55-65% (VPD range of 1.1-1.4 kPa) across measurements, but remained constant
371 during a particular measurement. Photosynthetically active radiation in the system is 1000 μmol
372 $\text{m}^{-2} \text{s}^{-1}$. Flow from the balance was monitored for 45 m to 1h until the flow rates reach steady
373 state. After the measurements, the leaf was detached and was put into a plastic bag to equilibrate
374 for 20 minutes to measure the leaf water potential (Model 1000, PMS Instrument, USA). K_{leaf}
375 values were further standardized to 25 °C and leaf area to make the K_{leaf} comparable among

376 studies and across species. Data indicating a sudden change of flow and whose leaf water
377 potential was an obvious outlier were deleted.

378

379 We measured pressure-volume (PV) curves for six leaves per species using the bench-drying
380 method^[43,44]. A leaf was cut directly from the same plants rehydrated in the lab (as described
381 above) using a razor blade and leaf water potential was measured immediately. Then, the leaf
382 weight was recorded. The leaf was initially allowed to dry on the bench for 2-minute intervals
383 and put into a ziplock bag and under darkness for 10-minute equilibration before measuring the
384 leaf water potential and leaf weight again. Then, the waiting intervals could be adjusted based on
385 the decrease of the leaf water potential (from 2 minutes-1h). Ideally, a decreasing gradient of -
386 0.2MPa for leaf water potential was obtained for the curves, until the leaf weight reached a
387 steady state. At the end of the experiment, leaves were dried in the oven at 70°C for 48h to obtain
388 the dry weight. The PV curves were used in curve fitting to obtain leaf capacitance, and leaf
389 turgor loss point using an excel program from Sack and Pasquet-Kok (2010)^[44].

390

391 Maximal assimilation rate (A_{\max}) and stomatal conductance (g_s) were measured under saturated
392 light intensity. A_{\max} and g_s were obtained using a standard 2 x 3 cm² leaf chamber with a red/blue
393 LED light source of LI-6400XT (LI-COR Inc., Lincoln, NE, USA). Light curves were measured
394 with light intensities of 2000, 1500, 1200, 1000, 800, 500, 300, 200, 150, 100, 75, 50, 20, 0 μmol
395 $\text{m}^{-2} \text{s}^{-1}$ under CO₂ of 400 ppm. Then, A_{\max} was estimated from the light curve^[45,46]. All the
396 measurements were made under the temperature of 25°C and the leaf temperature to air vapor
397 pressure deficit was controlled around 2kPa. g_s at the saturated light intensity of 2000 $\mu\text{mol} \text{m}^{-2}$
398 s^{-1} was recorded for each plant. The cuvette opening was covered by Fun-Tak to avoid and
399 correct for the leakiness.

400

401 *Phylogenetic analysis*

402 **Phylogenetic analysis for C₃ and C₄.** We pruned the dated phylogeny from a published grass
403 phylogeny to include only the species in our physiological experiments^[19](Fig. 1). Using the
404 dated phylogeny, for each of the hydraulic traits, we fitted evolutionary models to test which
405 evolutionary model best explains observed distribution of traits along the phylogeny and how
406 these models differ between C₃ and C₄ (Table S1). We fitted evolutionary models belonging

407 Brownian Motion model and Ornstein-Uhlenbeck Model using the package “mvMORPH” in
408 R^[47]. To determine the best fitted evolutionary model, we compared two criteria, the small-
409 sample-size corrected version of Akaike information criterion (AICc, the lower AICc, the better
410 fit) and Akaike weights (AICw, the higher AICw, the better fit)^[48,49,50]. The evolutionary models
411 have nested variants (Models 1-4; Models 5-6), varying in whether C₃ and C₄ species had the
412 same or different fluctuation rates, root states for Brownian motion model and optima for
413 Ornstein-Uhlenbeck model. We used likelihood-ratio test (LRT) to verify whether a specific
414 model variant performs significantly better. The AICc, AICw and LRT allowed us to test
415 evolutionary hypotheses, for instance, if the model in which C₃ and C₄ have different root states
416 fit significantly better than model in which C₃ and C₄ have the same root states, it means there is
417 a shift of physiological trait along with the formation of C₄. To examine the further evolution of
418 hydraulic traits after a full C₄ evolved, we extracted the evolutionary ages for each represented
419 C₄ origin from the dated phylogenetic trees. Then, we regressed the hydraulic traits with
420 evolutionary age. A significant negative correlation between evolutionary age and hydraulic trait
421 will indicate a further decreasing evolutionary direction after C₄ evolved. We also performed an
422 additional analysis to test the original states and further direction together. We extracted
423 molecular phylogeny for all the species from Edwards, GPWG II (2012)^[4]. Except for the six
424 evolutionary models mentioned above, the molecular phylogeny allows us to fit for additional six
425 Brownian motion models with trend (Supplementary Table S7). Likewise, if Brownian motion
426 model with trend fits the phylogenetic patterns better than Brownian motion model without trend
427 it means there is an evolutionary trend, and a significant LRT test for a two-trend model suggests
428 that C₃ and C₄ lineages differ in the speed or direction of hydraulic evolution. We also mapped
429 the traits on the phylogeny for potential further references (Fig. S2-S5).

430 To further test whether there are significant differences among C₄ subtypes, evolutionary models
431 with subtypes (Table S1) were used to fit the data. We again used AICc, AICw and LRT
432 methods to find the best model variants: whether there are significant differences for hydraulic
433 shifts and evolutionary trends among three different subtypes. For the leaf capacitance analysis,
434 *Dichanthelium clandestinum* is deleted as it is an obvious outlier.

435 **Phylogenetic analysis for correlations among traits.** Multivariate analysis in “mvMORPH”
436 was used to estimate the correlations between A_{\max} and each of the hydraulic traits and to test the

437 hypotheses that whether such correlations are different between C_3 and C_4 . The process of
438 brownian motion with different root for C_3 and C_4 was used for K_{leaf} , g_s and leaf turgor loss and
439 brownian motion with the same root was used for leaf capacitance. Since the Ornstein-
440 Uhlenbeck process is difficult to take the root state difference into consideration, here we used
441 Brownian motion assumptions as approximation for leaf turgor loss. Seven different correlation
442 models are fitted (Table S19). We used LRT for the seven correlation models to test whether the
443 correlation of the two traits is significantly different from 0 and whether the correlation of two
444 traits is significantly different between C_3 and C_4 . Such correlation analysis is similar to PGLS
445 considering C_3 and C_4 , but with more varieties on the setting of variance and covariance matrix.
446

447 ***Physiological Modeling***

448
449 Furthermore, we used physiological models that couples the photosynthesis systems and
450 hydraulic systems to predict the effect of changing K_{leaf} on assimilation rate^[32]. The change of
451 K_{leaf} was assumed to change the plant hydraulic conductance (K_{plant}) proportionally in the
452 modeling process. We double or reduce by half K_{leaf} relative to the original value to predict the
453 effects on assimilation rates for C_3 and C_4 pathways. We assumed C_4 had the same
454 photosynthetic properties with C_3 species (e.g., Rubisco affinity and specificity, Supplementary
455 Table S24) other than the carbon concentration mechanism, which mimics the initial evolution of
456 C_4 and the closely-related C_3 - C_4 system. We also model the additional scenarios in which C_4 had
457 different photosynthetic properties to support the above condition further (Supplementary Table
458 S25).

459

460 **Acknowledgements**

461 HZ and this research is supported by the NOAA Climate and Global Change Postdoctoral
462 Fellowship Program, administered by UCAR's Cooperative Programs for the Advancement of
463 Earth System Science (CPAESS) under award #NA18NWS4620043B and is also supported by
464 the Dissertation Completion Fellowship provided by the Graduate Division of School of Arts and
465 Sciences, University of Pennsylvania. BH is supported by NSF-IOS award 1856587.

466

467 **Data availability**

468 The data that support the findings of this study are available from the corresponding author upon
469 request.

470

471 **Code availability**

472 All source code is available upon request.

473

474

475 **References**

476

477 1. Sage, R.F., 2017. A portrait of the C₄ photosynthetic family on the 50th anniversary of its
478 discovery: species number, evolutionary lineages, and Hall of Fame. *Journal of*
479 *experimental botany*, 68(2), pp.e11-e28.

480 2. Ehleringer JR, Monson RK (1993). Evolutionary and ecological aspects of
481 photosynthesis pathway variation. *Annu Rev Ecol Syst* 24: 411-439.

482 3. Edwards, E. J. (2019). Evolutionary trajectories, accessibility and other metaphors: the
483 case of C₄ and CAM photosynthesis. *New Phytol.* 223(4), 1742-1755.

484 4. Grass Phylogeny Working Group II. (2012). New grass phylogeny resolves deep
485 evolutionary relationships and discovers C₄ origins. *New Phytol* 193: 304-312.

486 5. Christin PA, Osborne CP (2014) Tansley Review. The evolutionary ecology of
487 C₄ photosynthesis. *New Phytol* 204: 765-781.

488 6. Kocacinar F, Sage RF (2003) Photosynthetic pathway alters xylem structure and
489 hydraulic function in herbaceous plants. *Plant, Cell & Environment* 26(12): 2015-2026.

490 7. Pearcy RW, Ehleringer J (1984) Comparative ecophysiology of C₃ and C₄ plants. *Plant,*
491 *Cell & Environment* 7(1): 1-13.

492 8. Huxman TE, Monson RK (2003) Stomatal responses of C₃, C₃-C₄ and C₄ Flaveria species
493 to light and intercellular CO₂ concentration: implications for the evolution of stomatal
494 behaviour. *Plant, Cell & Environment* 26(2): 313-322.

495 9. Way DA, Katul GG, Manzoni S, Vico G (2014) Increasing water use efficiency along the
496 C₃ to C₄ evolutionary pathway: a stomatal optimization perspective. *Journal of*
497 *Experimental Botany* 65(13): 3683-3693.

498 10. Sack L, Frole K (2006) Leaf structural diversity is related to hydraulic capacity in
499 tropical rain forest trees. *Ecology* 87: 483-491.

500 11. Brodribb TJ, Feild TS, Jordan GJ (2007) Leaf maximum photosynthetic rate and venation
501 are linked by hydraulics. *Plant Physiol* 144: 1890-1898.

502 12. McKown AD, Cochard H, Sack L (2010) Decoding leaf hydraulics with a spatially
503 explicit model: principles of venation architecture and implications for its evolution. *Am*
504 *Nat* 175: 447-460.

505 13. Scoffoni C, Chatelet DS, Pasquet-kok J, Rawls M, Donoghue MJ, Edwards EJ, Sack L
506 (2016) Hydraulic basis for the evolution of photosynthetic productivity. *Nature*
507 *plants* 2:16072.

508 14. Osborne CP, Sack L (2012). Evolution of C₄ plants: a new hypothesis for an interaction of
509 CO₂ and water relations mediated by plant hydraulics. *Philos Trans R Soc Lond B Biol*
510 *Sci* 367: 583-600.

- 511 15. Griffiths H, Weller G, Toy L, Dennis RJ (2012) You're so vein: bundle sheath physiology,
512 phylogeny and evolution in C₃ and C₄ plants. *Plant Cell Environ* 36: 249–261.
- 513 16. Sage RF (2001) Environmental and evolutionary preconditions for the origin and
514 diversification of the C₄ photosynthetic syndrome. *Plant Biology* 3: 202-213.
- 515 17. McCulloh, KA, Sperry, JS, Adler, FR (2003) Water transport in plants obeys Murray's
516 law. *Nature* 421: 939-942.
- 517 18. Sage RF, Sage TL, Kocacinar F (2012) Photorespiration and the evolution of C₄
518 photosynthesis. *Annual review of plant biology* 63: 19-47.
- 519 19. Spriggs EL, Christin PA and Edwards EJ (2014) C₄ photosynthesis promoted species
520 diversification during the Miocene grassland expansion. *Plos one* 9(5): p.e97722.
- 521 20. Heyduk ., Moreno-Villena JJ, Gilman IS, Christin PA, and Edwards EJ (2019). The
522 genetics of convergent evolution: insights from plant photosynthesis. *Nature Review*
523 *Genetics*, 20, 485-493.
- 524 21. Martre P, Cochard H, Durand JL (2001) Hydraulic architecture and water flow in
525 growing grass tillers (*Festuca arundinacea* Schreb.). *Plant, Cell and Environment* 24: 65–
526 76.
- 527 22. Ocheltree TW, Nippert JB, Prasad PV (2016) A safety vs efficiency trade-off identified in
528 the hydraulic pathway of grass leaves is decoupled from photosynthesis, stomatal
529 conductance and precipitation. *New Phytologist* 210(1): 97-107.
- 530 23. Liu H, Osborne CP (2015) Water relations traits of C₄ grasses depend on phylogenetic
531 lineage, photosynthetic pathway, and habitat water availability. *Journal of Experimental*
532 *Botany* 66, 761–773.
- 533 24. Liu H, Taylor SH, Xu Q, Lin Y, Hou H, Wu G, Ye, Q (2019) Life history is a key factor
534 explaining functional trait diversity among subtropical grasses, and its influence differs
535 between C₃ and C₄ species. *Journal of experimental botany* 70(5): 1567-1580.
- 536 25. Taylor SH, Hulme SP, Rees M, Ripley BS, Woodward FI, Osborne CP (2010).
537 Ecophysiological traits in C₃ and C₄ grasses: a phylogenetically controlled screening
538 experiment *New Phytol* 185: 780-791
- 539 26. Taylor SH, Franks PJ, Hulme SP, Spriggs E, Christin PA, Edwards EJ, Woodward FI,
540 Osborne CP (2012) Photosynthetic pathway and ecological adaptation explain stomatal
541 trait diversity amongst grasses. *New Phytol* 193: 387-396.
- 542 27. Sage RF (2004) The evolution of C₄ photosynthesis. *New Phytol* 161(2):341-370.
- 543 28. Christin PA, Osborne CP, Chatelet DS, Columbus JT, Besnard G, Hodkinson TR,
544 Garrison LM, Vorontsova MS, Edwards EJ (2013) Anatomical enablers and the evolution
545 of C₄ photosynthesis in grasses. *Proc Natl Acad Sci USA* 110: 1381-1386.
- 546 29. Lundgren MR, Besnard G, Ripley BS, Lehmann CE, Chatelet DS, Kynast RG,
547 Namaganda M, Vorontsova MS, Hall RC, Elia J, Osborne CP (2015) Photosynthetic
548 innovation broadens the niche within a single species. *Ecology Letters* 18(10): 1021-
549 1029.
- 550 30. Sage RF, Monson RK, Ehleringer JR, Adachi S, Percy RW (2018) Some like it hot: the
551 physiological ecology of C₄ plant evolution. *Oecologia* 187(4):941-966.
- 552 31. Brodribb TJ, Holbrook NM, Zwieniecki MA, Palma B (2005) Leaf hydraulic capacity in
553 ferns, conifers and angiosperms: impacts on photosynthetic maxima. *New Phytol* 165:
554 839–846
- 555 32. Zhou H, Helliker BR, Huber M, Dicks A, Akçay E (2018) C₄ photosynthesis and climate
556 through the lens of optimality. *Proceedings of the National Academy of Sciences* 115:

- 557 12057-12062.
- 558 33. Ripley BS, Cunniff J, Osborne CP (2013) Photosynthetic acclimation and resource use by
559 the C₃ and C₄ subspecies of *Alloteropsis semialata* in low CO₂ atmospheres. *Glob*
560 *Change Biol* 19: 900–910.
- 561 34. Taylor SH, Ripley BS, Martin T, De-Wet L-A, Woodward FI, Osborne CP (2014).
562 Physiological advantages of C₄ grasses in the field: a comparative experiment
563 demonstrating the importance of drought. *Glob Change Biol* 20: 1922-2003.
- 564 35. Tyree MT, Sperry JS (1989) Vulnerability of xylem to cavitation and embolism. *Annu*
565 *Rev Plant Physiol Plant Mol Biol* 40(1):19–36.
- 566 36. Niinemets Ü, Portsmouth A, Tobias M (2007) Leaf shape and venation pattern alter the
567 support investments within leaf lamina in temperate species: a neglected source of leaf
568 physiological differentiation? *Functional Ecology* 21: 28-40.
- 569 37. Scoffoni C, Rawls M, McKown A, Cochard H, Sack L (2011) Decline of leaf hydraulic
570 conductance with dehydration: relationship to leaf size and venation architecture. *Plant*
571 *Physiology* 156(2): 832-843.
- 572 38. Wolf A, Anderegg WR, Pacala SW (2016) Optimal stomatal behavior with competition
573 for water and risk of hydraulic impairment. *Proceedings of the National Academy of*
574 *Sciences* 113(46): E7222-E7230.
- 575 39. Scoffoni C, Albuquerque C, Brodersen CR, Townes SV, John GP, Bartlett MK, Buckley
576 TN, McElrone AJ, Sack L (2017) Outside-xylem vulnerability, not xylem embolism,
577 controls leaf hydraulic decline during dehydration. *Plant Physiology* 173: 1197-1210.
- 578 40. Pathare VS, Sonawane BV, Koteyeva N, Cousins AB (2020) C₄ grasses adapted to low
579 precipitation habitats show traits related to greater mesophyll conductance and lower leaf
580 hydraulic conductance. *Plant Cell & Environment* doi: 10.1111/pce.13807.
- 581 41. Sack L, Scoffoni C (2012) Measurement of Leaf Hydraulic Conductance and Stomatal
582 Conductance and Their Responses to Irradiance and Dehydration Using the Evaporative
583 Flux Method (EFM). *J Vis Exp* (70), e4179, doi:10.3791/4179.
- 584 42. Ocheltree T, Gleason S, Cao KF, Jiang GF (2020) Loss and recovery of leaf hydraulic
585 conductance: Root pressure, embolism, and extra-xylary resistance. *Journal of Plant*
586 *Hydraulics* 7
- 587 43. Tyree MT, Hammel HT (1972) The measurement of the turgor pressure and the water
588 relations of plants by the pressure-bomb technique. *Journal of Experimental*
589 *Botany* 23(1): 267-282.
- 590 44. Sack L, Pasquet-Kok J and PrometheusWiki contributors. Leaf pressure-volume curve
591 parameters. PrometheusWiki. May 20, 2010, 17:08 UTC. Available at: /wiki-
592 pagehistory.php?page=Leaf pressure-volume curve parameters&preview=16.
- 593 45. Marshall B, Biscoe PV (1980) A model for C₃ leaves describing the dependence of net
594 photosynthesis on irradiance. *Journal of Experimental Botany* 31:29-39.
- 595 46. Thornley JHM (1998) Dynamic model of leaf photosynthesis with acclimation to light
596 and nitrogen. *Annals of Botany* 81(3): 421-430.
- 597 47. Clavel J, Escarguel G, Merceron G (2015) mvMORPH: an R package for fitting
598 multivariate evolutionary models to morphometric data. *Methods in Ecology and*
599 *Evolution*, 6(11):1311-1319.<doi:10.1111/2041-210X.12420>
- 600 48. Akaike H (1974) A new look at the statistical model identification. In *Selected Papers of*
601 *Hirotsugu Akaike* (pp. 215-222). Springer, New York, NY.
- 602 49. Cavanaugh JE (1997) Unifying the derivations for the Akaike and corrected Akaike

603 information criteria. *Statistics & Probability Letters* 33(2): 201-208.
604 50. Burnham KP and Anderson DR (1998) Practical use of the information-theoretic
605 approach. In *Model Selection and Inference* (pp. 75-117). Springer, New York, NY.
606